# MULTI-COUNTERPROPAGATION NETWORK MODEL FOR COLOUR RECOGNITION 

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#### Abstract

Minolta Chroma Meters was used to convert colours into numbers. It offers five different colour systems for measuring absolute chromaticity, that is, CIE Yxy, $L^{*} a^{*} b^{*}$, $L^{*} C^{*} H^{0}$, Hunter Lab and XYZ. In this study, only $L^{*} a^{*} b^{*}$ is used, and combinations of two counterpropagation network (CPN) are required to recognise 808 colours produced by The Royal Horticultural Society, based on RHS Colour Chart [1]. Our proposed neural network model is tested; the result shows that $99 \%$ of trained data are recognised, against $98 \%$ for untrained data.


Keywords: CPN model, competitive layer, unsupervised learning, supervised learning, Minolta Chroma Meters

### 1.0 INTRODUCTION

An infinite number of colours surround us in our everyday lives. We take colour pretty much for granted, but its role in our daily lives ranges from influencing our tastes in food and other purchases to telling us whether plants are healthy or not.

The need for an automatic colour recognition system for industrial and commercial applications is very widespread. Existing examples include colour coding in the manufacturing of electrical equipment, colour matching of tones in tanneries and paints in the automotive industry, colour recognition as an aid for the blind and colour-blind, and colour recognition as a powerful and reliable parameter for object recognition in robotics. Specific examples include diamond color sorting and quality control for the manufacturing of coloured paper [2].

Colour is a matter of perception, of subjective interpretation. To express the same colour, different people
draw upon different references and express the exact same colour in different words. It is because there are such varied expressions that communicating a particular colour is so difficult and vague.

### 1.1 Colours

Colour is a visual object attribute, which results from combined output of three sets of retinal cones, each sensitive to different portions of the visible part of the electromagnetic spectrum. The cones have peak sensitivities in the red, green and blue portions of the spectrum, respectively. Any perceived colour may usually be created by a variety of sets of "primary" colours when combined in the correct proportions.

Colours are generally described by hue, value and chroma [2]. Hue is the combination of different wavelengths that produce a colour. Value is lightness or intensity and depends on the amount of energy present in all the wavelengths of a colour; this is not however the same as the luminance of a colour. Chroma is saturation whereby saturation can be described as the purity of a colour, and indicates the range of wavelengths around the colour wavelength in which most of the energy is present. Therefore, a single wavelength would have a high saturation, whereas a colour consisting of a number of wavelengths would have a low saturation.

Hue, value and chroma can be visualized in three dimensions as shown Fig. 1. Colour hues are on the outside around the central axis, with value forming the vertical axis and chroma the horizontal axis from the centre. If the three attributes shown in Fig. 1 were actually combined into a three-dimensional system, they would appear as a colour solid. Because the chroma steps on the horizontal axis vary with each hue and value, the final solid assumes a fairly complicated configuration. When expressed in a figure, the
relationship between hue, value and chroma becomes much clearer [3].

### 1.2 Counter Propagation Network (CPN)

Neural networks are mathematical models of the way in which neurons (hence the name) in the brain fire and interact. Just as the brain learns by strengthening connections between neurons, so do neural networks, which can also be trained. Typical functions for neural networks include learning functions such as time-series, recognition tasks (image recognition etc.), extraction of features within data (data mining), statistical clustering (statistical correlation) and predictive functions, such as sales predictions.

A CPN is a multilayer network based on a combination of input, clustering, and output layer. CPN can be used to compress data, to approximate functions, or to associate patterns. CPN provides an excellent example of a network that combines different layer from other paradigms to construct a new type of network. Two different types of layer are used in CPN: the hidden layer is a Kohonen layer,
with competitive units that do unsupervised learning; the top layer is the Grossberg layer, which is fully interconnected to the hidden layer, and is not competitive. The Grossberg layer is trained by a Widrow-Hoff or Grossberg rule [4].

In supervised learning, there is a "teacher" who in the learning phase "tells" the net how well it performs ("reinforcement learning") or what the correct behavior should have been ("fully supervised learning"). In unsupervised learning, the net is autonomous: it just looks at the data it is presented with, finds out about some of the properties of the data set, and learns to reflect these properties in its output. What exactly these properties are, that the network can learn to recognise, depends on the particular network model and learning method.

Fig. 2 shows the topology of a typical three-layered CPN. The first layer of units is solely for input, the second is the competitive-Kohonen layer, and the third is the layer of output units (the Grossberg layer). Each layer is fully interconnected to the layer above it [4].


Fig. 1: Three-Dimension (3D) Colour System


Fig. 2: A Three-layer CPN


Fig. 3: Training a Localised Neighbourhood


Fig 4: Architecture of Multi-CPN

At the competitive layer (Kohonen layer), Kohonen introduces the idea of topological neighbourhoods which is a dynamically changing boundary that defines how many nodes surrounding the winning node will be affected with weight modifications during the training process.

Fig. 3 shows the effect of shrinking the neighbourhood by localising areas of similar activity. All the units with the shaded area in A are initially affected, and realign themselves slightly towards the winning node's weight vector. As time passes, the neighbourhood is reduced and only the nodes in the neighbourhood of the winning node are altered. These latter align themselves more and more, until the area around the winner consists of similar weight vectors. In the resulting network, an input which is close to the one that triggered the original node will elicit a response from a node that is topogically closed [5].

### 2.0 COLOUR RECOGNITION AND MULTI-CPN MODEL

The $L^{*} \mathrm{a}^{*} \mathrm{~b}^{*}$ colour system is presently one of the most popular colour systems for measuring object colour, and is widely used in all fields. In this colour system, $L^{*}, a^{*}$ and $\mathrm{b}^{*}$ are the three coordinates that can be put together to
create the three-dimensional colour solids as shown in Fig. 1. The $L^{*}$ coordinates indicate the lightness which forms the vertical axis with values ranging from 0 (black) to 100 (white). The $a^{*}$ and $b^{*}$ coordinates form the horizontal axis, whereby their coordinates are redness $\left(+a^{*}\right)$ to greenness $\left(-\mathrm{a}^{*}\right)$, and yellowness $\left(+\mathrm{b}^{*}\right)$ to blueness $\left(-\mathrm{b}^{*}\right)$. The $\mathrm{a}^{*}$ and $\mathrm{b}^{*}$ coordinates are used to calculate the hue angle ( $\mathrm{h}^{\circ}$ ) and chroma ( $\mathrm{C}^{*}$ ) [3].

Running CPN using 100 colours as input [6], will take 24 minute 43.32 seconds for $100 \%$ recognition for trained and untrained data. But, if trained with 808 colours produced by The Royal Horticultural Society, it required a large size of memory and the training process took quite a time. So, to solve this problem, two combined CPNs models are proposed; the main CPN and a second CPN. The main CPN has three input nodes and seven output nodes. These seven output nodes represent seven groups of colours. The second CPN is the group that, for each colour, consists of seven CPNs. Fig. 4 shows the architecture of the multineural network.

### 3.0 METHODOLOGY

In multi-CPN, 808 colours will be divided into seven groups. Each group has different amount of data, as shown in Table 1.

Table 1: Groups of Data for Second CPNs

| Group | Amount of data <br> (colours) |
| :---: | :---: |
| 1 | 140 |
| 2 | 156 |
| 3 | 96 |
| 4 | 104 |
| 5 | 120 |
| 6 | 36 |
| 7 | 156 |
| Total | 808 |

The algorithm for multi-CPN model as follows:
Step 1. Each group of second CPN runs separately with the same initial neighbourhood, size of competitive layer and the number of cycles to get their respective weights.
Step 2. The main CPN will run after the second CPN finish.
Step 3. Recalls the data using the final weight.
The learning rule for weights $\left(v_{i J}, i=1,2, \ldots, m\right.$ and $J=1,2, \ldots, n$ ) from input units $\left(x_{i}, i=1,2, \ldots, m\right)$ to competitive units $\left(z_{j}, j=1,2, \ldots, q\right)$ [7] is

$$
\begin{aligned}
& v_{i J}(\text { new })=v_{i J}+\alpha\left(x_{i}-v_{i J}\right) \\
& =(1-\alpha) v_{i J}(\text { old })+\alpha x_{i}
\end{aligned}
$$

and the learning rule for weights $\left(w_{J k}, J=1,2, \ldots, n\right.$ and $\mathrm{k}=1,2, \ldots, p$ ) from competitive units to output units $\left(y_{k}\right.$, $k=1,2, \ldots, p)$ is

$$
\begin{aligned}
w_{J k}(\text { new }) & =w_{J k}+\mathrm{a}\left(y_{k}-w_{j k}\right) \\
& =(1-\mathrm{a}) w_{J_{k}}(\text { old })+\mathrm{a} y_{k}
\end{aligned}
$$

However, if $\mathrm{w}_{j k}$ is interpreted as the computed output (i.e., $\mathrm{y}_{k}=\mathrm{w}_{j k}$ ), and the activation of the competitive units is included as

$$
z_{j}=1 \text { if } j=\mathrm{J}
$$

$$
\text { or } \quad z_{j}=0 \text { if } j \neq \mathrm{J}
$$

then, the learning rule for the weights from the competitive units to the output units can be written in the form of delta rule:

$$
w_{j k}(\text { new })=w_{j k}+\mathrm{a} z_{j}\left(y_{k}-w_{j k}\right)
$$

### 4.0 RESULTS AND DISCUSSION

Data used for the training phase were taken from the Minolta Chroma Meters that can convert colours into numbers, see Table A01 in Appendix A. The data were then normalised within the range of -1 and 1 using the formula

$$
\mathrm{D}_{s c l}=\mathrm{R}_{\min }+\left(\mathrm{R}_{\max }-\mathrm{R}_{\min }\right) \times\left(\mathrm{D}-\mathrm{D}_{\min }\right) /\left(\mathrm{D}_{\max }-\mathrm{D}_{\min }\right)
$$

where

| D | real data |
| :--- | :--- |
| $\mathrm{D}_{\text {scl }}$ | scale data |
| $\mathrm{D}_{\text {min }}$ | minimum value from set of data |
| $\mathrm{D}_{\text {max }}$ | maximum value from set of data |
| $\mathrm{R}_{\text {min }}$ | minimum value from a range |
| $\mathrm{R}_{\text {max }}$ | maximum value from a range |

For the initial experiment, 100 colours will be run first to see the effectiveness of multi-CPN. The results show (Table 2) that all experiments get $100 \%$ recognition for trained and untrained data.

From Table 2 and Table 3, it is shown that multi-CPN can recognise much better than CPN and that the training time is faster than for CPN [6]. Then, the data was increased to 808. The results are shown from Table 4 to Table 9, and CPN1 is the first part of multi-CPN, whereas CPN2 is the second part of multi-CPN.

Table 2: Percentage of Recognition Multi-CPN (100 colours) with Initial Neighbourhood are 5 and Size of Competitive Layer are 500

|  | No. of Cycle |  |  |
| :---: | :---: | :---: | :---: |
| Set of Data | 100 | 300 | 500 |
| Trained | 100 | 100 | 100 |
| Untrained | 100 | 100 | 100 |
| Time Taken for Training | $0: 00: 14.93$ | $0: 00: 43.97$ | $0: 01: 16.55$ |

Table 3: Percentage of Recognition Multi-CPN (100 colours) with Initial Neighbourhood are 10 and Size of Competitive Layer are 500

|  | No. of Cycle |  |  |
| :---: | :---: | :---: | :---: |
| Set of Data | 100 | 300 | 500 |
| Trained | 100 | 100 | 100 |
| Untrained | 100 | 100 | 100 |
| Time Taken for Training | $0: 00: 15.1$ | $0: 00: 45.31$ | $0: 01: 15.55$ |

From Table 4, it can be seen that, when the number of cycles was increased from 1000 to 2000, percentage recognition for trained data increased of about $0.2 \%$. Untrained data, however, decreased of about $0.5 \%$. When the number of cycles was increased from 2000 to 5000 , percentage recognition decreased of about $1.5 \%$ for trained data, and $1.2 \%$ for untrained data. This may have been caused by an extreme value of the initial neighbourhood.

After that, when the initial neighbourhood was increased from 10 to 12 , and the size of competitive layer kept to 1000 (Table 5), the percentage recognition decreased for each number of cycle. It shows here that, when the initial neighbourhood is increased, it does not mean that the percentage of recognition will also increase. For the next step, the initial neighbourhood was kept at 10 , and the size of competitive layer was increased from 1000 to 1500 (Table 6). At this level, the percentage of recognition for trained and untrained data increased.

From Table 7, the results show that when the initial neighbourhood was increased from 10 to 12 , and the
competitive layer were kept to 1500 , for a number of cycles of 1000 , percentage recognition for trained data still remained $96.8 \%$. However, untrained data increased of about $0.4 \%$. When the number of cycles was increased from 1000 to 2000, percentage recognition for trained data increased from $96.8 \%$ to $97.0 \%$ and, for untrained data, it increased from $95.4 \%$ to $95.8 \%$. Percentage recognition for trained data increased of about $0.3 \%$, and about $0.6 \%$ for untrained data when the number of cycles was increased from 2000 to 5000 .

When the competitive layer were increased from 1500 to 2000 and the initial neighbourhood kept at 10, percentage recognition for trained data increased of about $0.8 \%, 1.3 \%$ and $0.8 \%$ for number of cycles of 1000,2000 and 5000, respectively.

From Table 9, the results show that multi-CPN can recognise up to $99.3 \%$ for trained data, and $98.4 \%$ for untrained data. This means that, from 808 colours, 802 were recognised for trained data, and 795 for untrained data.

Table 4: Percentage of Recognition Multi-CPN (808 colours) with Initial Neighbourhood are 10 and Size of Competitive Layer are 1000

|  | No. of Cycle |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1000 |  |  | 2000 |  | 5000 |  |
| Set of Data | CPN1 | CPN2 | CPN1 | CPN 2 | CPN1 | CPN 2 |  |
| Trained | 91 | 91 | 91.2 | 91.2 | 89.7 | 89.7 |  |
| Untrained | 90.6 | 90.6 | 90.1 | 90.1 | 88.9 | 88.9 |  |
| Time taken for training | $0: 39: 25.71$ |  | $1: 18: 46.03$ | $2: 41: 52.12$ |  |  |  |

Table 5: Percentage of Recognition Multi-CPN (808 colours) with Initial Neighbourhood are 12 and Size of Competitive Layer are 1000

|  | No. of Cycle |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1000 |  |  | 2000 |  | 5000 |  |
| Set of Data | CPN1 | CPN2 | CPN 1 | CPN 2 | CPN 1 | CPN 2 |  |
| Trained | 88.1 | 88.1 | 90.3 | 90.3 | 89.0 | 89.0 |  |
| Untrained | 87.4 | 87.4 | 89.6 | 89.6 | 88.5 | 88.5 |  |
| Time taken for training | $0: 39: 41.77$ |  | $1: 19: 17.37$ |  | $2: 48: 06.45$ |  |  |

Table 6: Percentage of Recognition Multi-CPN (808 colours) with Initial Neighbourhood are 10 and Size of Competitive Layer are 1500

|  | No. of Cycle |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1000 |  |  | 2000 |  | 5000 |  |
| Set of Data | CPN1 | CPN2 | CPN1 | CPN2 | CPN1 | CPN2 |  |
| Trained | 96.8 | 96.8 | 96.3 | 96.3 | 96.9 | 96.9 |  |
| Untrained | 95.8 | 95.8 | 95.3 | 95.3 | 95.9 | 95.9 |  |
| Time taken for training | $0: 49: 05.25$ |  | $1: 36: 02.25$ | $4: 04: 01.59$ |  |  |  |

Table 7: Percentage of Recognition Multi-CPN (808 colours) with Initial Neighbourhood are 12 and Size of Competitive Layer are 1500

|  | No. of Cycle |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1000 |  |  |  |  |  |  | 2000 |  | 5000 |  |
| Set of Data | CPN1 | CPN2 | CPN1 | CPN2 | CPN1 | CPN2 |  |  |  |  |  |
| Trained | 96.8 | 96.8 | 97 | 97 | 97.3 | 97.3 |  |  |  |  |  |
| Untrained | 95.4 | 95.4 | 95.8 | 95.8 | 96.4 | 96.4 |  |  |  |  |  |
| Time taken for training | $0: 49: 01.06$ | $1: 36: 32.08$ | $4: 00: 17.68$ |  |  |  |  |  |  |  |  |

Table 8: Percentage of Recognition Multi-CPN (808 colours) with Initial Neighbourhood are 10 and Size of Competitive Layer are 2000

|  | No. of Cycle |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1000 |  |  |  |  |  |
| CPN1 | CPN2 | CPN1 | CPN2 | CPN 1 | CPN 2 |  |
| Set of Data | 97.6 | 97.6 | 98.3 | 98.3 | 98.1 | 98.1 |
| Trained | 96.9 | 96.9 | 97.5 | 97.5 | 97.4 | 97.4 |
| Untrained | $1: 04: 47.12$ |  | $2: 10: 19.24$ | $5: 20: 16.64$ |  |  |

Table 9: Percentage of Recognition Multi-CPN (808 colours) with Initial Neighbourhood are 12 and Size of Competitive Layer are 2000

|  | No. of Cycle |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1000 |  |  |  |  |  |  | 2000 |  | 5000 |  |
| Set of Data | CPN1 | CPN2 | CPN1 | CPN2 | CPN1 | CPN2 |  |  |  |  |  |
| Trained | 98.3 | 98.3 | 99.3 | 99.3 | 99.0 | 99.0 |  |  |  |  |  |
| Untrained | 97.4 | 97.4 | 98.4 | 98.4 | 98.0 | 98.0 |  |  |  |  |  |
| Time taken for training | $1: 09: 11.16$ | $2: 10: 26.20$ | $5: 29: 53.49$ |  |  |  |  |  |  |  |  |

From Fig. 5(a), 5(b) and, 5(c), for parameters A and B, with size of competitive layer at 1000, the average of percentage recognition for trained data was about $89.88 \%$, and about $89.18 \%$ for untrained data. Parameters C and D, with size of competitive layer at 1500 generated an average of percentage recognition of about $96.85 \%$ for trained data and $95.77 \%$ for untrained data. Averages of percentage for trained and untrained data for parameters E and F are $98.43 \%$ and $97.6 \%$, respectively.

Fig. 6 shows that, for the initial stage, the number of cycles with 1000 gives a better performance than the number of cycles with 5000 . But, at the final stage, percentage recognition for the number of cycles with 5000 becomes $99 \%$ for trained data, compared to the number of cycles with 1000 which becomes $98.3 \%$ for trained data, as well. However, the number of cycles with 2000 are much better than the number of cycles with 5000 , whereby, for the initial stage, the number of cycles with 2000 got $91.2 \%$ recognition for trained data and, at the final stage, got $99.3 \%$ for trained data, whereas the number of cycles with 5000 got $89.7 \%$ recognition for trained data at the initial stage and $99 \%$ recognition for trained data at the final stage.

### 5.0 CONCLUSION

From this study, it shows that, if the number of cycles were increased or decreased, this causes over learning or not enough learning for the network. Also, if the initial neighbourhood is too small, it causes the competitive nodes that have the same potential to be neglected. However, if the initial neighbourhood is too big, the time of learning increases. The optima values of the number of cycles, the initial neighbourhood and the size of the competitive layer are very important in order to have a good percentage of recognition.

The results show that training with multi-CPN is able to produce a satisfying output with $99.3 \%$ recognition for trained data, that is, from 808 colours which were tested, about 802 were recognised, and $98.4 \%$ recognition for untrained data, that is, about 795 out of 808 colours were recognised.

(a) 1000 Cycles


(b) 2000 Cycles

Parameters

|  | Initial Neighbourhood | Size of Competitive Layer |
| :---: | :---: | :---: |
| A | 10 | 1000 |
| B | 12 | 1000 |
| C | 10 | 1500 |
| D | 12 | 1500 |
| E | 10 | 2000 |
| F | 12 | 2000 |

© 5000 Cycles

Fig. 5: Percentage of Recognition for Multi-CPN with 808 Colours


| Parameters |  |  |
| :---: | :---: | :---: |
|  | Initial Neighbourhood | Size of Competitive Layer |
| A | 10 | 1000 |
| B | 12 | 1000 |
| C | 10 | 1500 |
| D | 12 | 1500 |
| E | 10 | 2000 |
| F | 12 | 2000 |

$-\square-$ No. of Cycle are 1000

- No. of Cycle are 2000
- No. of Cycle are 5000

Fig. 6: Percentage of Recognition vs Initial Neighbourhood and Competitive Layer Representations

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## APPENDIX A

Table A01 : Samples of 808 Colours Before and After Normalisation

| Name of Colour | Samples of Input Before Normalised |  |  | Samples of Input After Normalised |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| RHS1A_BRILLIANT_GREENISH_YELLOW | 89.67 | -15.41 | 66.60 | 0.2487 | 0.2037 | 0.4643 |
| RHS1B_BRILLIANT_GREENISH_YELLOW | 89.17 | -18.42 | 61.64 | 0.5615 | -0.0409 | 0.7237 |
| RHS1C_LIGHT_YELLOW_GREEN | 91.55 | -14.68 | 41.28 | 0.7174 | -0.2150 | 0.8448 |
| RHS1D_PALE_GREENISH_YELLOW | 93.38 | -10.21 | 33.05 | 0.9434 | -0.5715 | 1.0000 |
| RHS2A_BRILLIANT_GREENISH_YELLOW | 90.07 | -12.20 | 70.11 | 0.3914 | -0.0710 | 0.3407 |
| RHS2B_BRILLIANT_GREENISH_YELLOW | 91.22 | -14.01 | 61.54 | 0.6425 | -0.3401 | 0.5393 |
| RHS2C_LIGHT_GREENISH_YELLOW | 93.53 | -11.87 | 39.75 | 0.8194 | -0.5252 | 0.7430 |
| RHS2D_PALE_GREENISH_YELLOW | 93.12 | -7.80 | 28.44 | 0.9983 | -0.7336 | 0.9373 |
| RHS3A_BRILLIANT_GREENISH_YELLOW | 90.40 | -10.90 | 68.20 | -0.6821 | 0.3424 | 0.3082 |
| RHS3B_BRILLIANT_GREENISH_YELLOW | 91.60 | -11.96 | 62.28 | -0.2070 | 0.3778 | 0.2426 |
| RHS3C_LIGHT_GREENISH_YELLOW | 92.52 | -11.12 | 47.93 | 0.2894 | 0.1283 | 0.4586 |
| RHS3D_LIGHT_GREENISH_YELLOW | 93.97 | -9.79 | 38.44 | 0.4748 | -0.0703 | 0.5883 |
| RHS4A_BRILLIANT_GREENISH_YELLOW | 91.56 | -12.30 | 62.26 | -0.5900 | 1.0000 | 0.0493 |
| RHS4B_LIGHT_GREENISH_YELLOW | 93.12 | -11.48 | 50.51 | -0.2762 | 0.7377 | 0.1261 |
| RHS4C_LIGHT_GREENISH_YELLOW | 93.89 | -9.28 | 40.42 | 0.0959 | 0.3394 | 0.3162 |
| RHS4D_PALE_YELLOW_GREEN | 94.69 | -5.36 | 21.58 | 0.3487 | 0.0658 | 0.4718 |
| RHS5A_BRILLIANT_GREENISH_YELLOW | 88.68 | -9.38 | 69.67 | -0.9122 | -0.4260 | 0.6906 |
| RHS5B_BRILLIANT_GREENISH_YELLOW | 90.63 | -10.34 | 68.90 | -0.8353 | -0.2761 | 0.5129 |
| RHS5C_LIGHT_GREENISH_YELLOW | 92.49 | -10.43 | 54.40 | -0.6886 | -0.0601 | 0.3874 |
| RHS5D_PALE_GREENISH_YELLOW | 93.85 | -7.62 | 38.62 | -0.4700 | -0.1328 | 0.4473 |
| RHS6A_BRILLIANT_GREENISH_YELLOW | 89.99 | -7.20 | 72.50 | -0.5391 | 0.8651 | -0.1771 |
| RHS6B_BRILLIANT_GREENISH_YELLOW | 90.33 | -7.77 | 69.79 | -0.1854 | 0.5530 | -0.0021 |
| RHS6C_BRILLIANT_GREENISH_YELLOW | 91.73 | -8.28 | 62.72 | 0.1952 | 0.1815 | 0.2389 |
| RHS6D_LIGHT_GREENISH_YELLOW | 93.21 | -7.03 | 42.78 | 0.3409 | 0.0126 | 0.3601 |
| RHS7A_BRILLIANT_GREENISH_YELLOW | 86.16 | -6.17 | 73.68 | -0.6937 | 0.8474 | -0.3148 |
| RHS7B_BRILLIANT_GREENISH_YELLOW | 89.62 | -6.28 | 67.15 | -0.3738 | 0.6959 | -0.2214 |
| RHS7C_BRILLIANT_GREENISH_YELLOW | 90.79 | -7.94 | 66.70 | 0.0617 | 0.2553 | 0.0922 |
| RHS7D_LIGHT_GREENISH_YELLOW | 92.16 | -9.03 | 55.41 | 0.2918 | 0.0254 | 0.2709 |
| RHS8A_BRILLIANT_GREENISH_YELLOW | 90.98 | -6.65 | 65.49 | -0.5632 | 0.6397 | -0.5624 |
| RHS8B_LIGHT_YELLOW | 92.09 | -7.27 | 55.34 | -0.1962 | 0.2941 | -0.2450 |
| RHS8C_LIGHT_YELLOW | 92.97 | -6.29 | 41.58 | 0.0915 | 0.0288 | 0.0163 |
| RHS8D_PALE_YELLOW | 94.02 | -4.15 | 23.29 | 0.2931 | -0.1438 | 0.1959 |
| RHS9A_VIVID | 88.85 | -4.39 | 78.22 | -0.8689 | -0.1773 | 0.3685 |
| RHS9B_BRILLIANT_YELLOW | 89.96 | -5.30 | 73.49 | -0.7255 | 0.0823 | 0.1540 |
| RHS9C_BRILLIANT_YELLOW/LIGHT_YELLOW | 91.65 | -7.13 | 58.94 | -0.5368 | -0.0073 | 0.1210 |
| RHS9D_PALE_YELLOW | 93.33 | -5.06 | 33.28 | -0.3456 | 0.0699 | 0.0587 |
| RHS10A_LIGHT_YELLOW | 89.98 | -5.09 | 56.58 | -0.1786 | 0.1208 | 0.0153 |
| RHS10B_LIGHT_YELLOW | 90.55 | -5.54 | 49.72 | 0.2938 | 0.0560 | 0.3634 |
| RHS10C_LIGHT_YELLOW | 91.57 | -5.72 | 42.47 | 0.5896 | -0.2670 | 0.5992 |
| RHS10D_PALE_YELLOW | 93.70 | -4.85 | 27.61 | 0.8160 | -0.6898 | 0.7015 |
| RHS11A_BRILLIANT_YELLOW | 86.36 | -2.21 | 58.71 | 0.1701 | -0.3635 | 0.2912 |
| RHS11B_LIGHT_YELLOW | 88.66 | -3.67 | 43.76 | 0.3351 | -0.4909 | 0.2488 |
| RHS11C_PALE_YELLOW | 91.12 | -3.33 | 32.13 | 0.5388 | -0.4603 | 0.3289 |
| RHS11D_PALE_YELLOW/YELLOWISH_WHITE | 93.84 | -1.92 | 17.09 | 0.8638 | -0.7377 | 0.7095 |
| RHS12A_BRILLIANT_YELLOW | 88.43 | -1.77 | 74.67 | -0.8197 | -0.0865 | 0.1648 |
| RHS12B_BRILLIANT_YELLOW | 89.59 | -4.21 | 66.10 | -0.5581 | 0.0375 | -0.0842 |
| RHS12C_LIGHT_YELLOW | 91.41 | -3.70 | 50.36 | -0.3494 | -0.0514 | -0.0719 |
| RHS12D_PALE_YELLOW | 92.48 | -2.32 | 32.31 | -0.1461 | -0.1506 | -0.0516 |

